

## L'equilibrio nel modello IS-LM

We derived the IS and LM equation as:

$$IS: i = \left(\frac{1}{f}\right)\bar{A} - \left(\frac{1-c}{f}\right)Y \quad (1)$$

$$LM: i = \frac{1}{h} [kY - \bar{M}] \quad (2)$$

Equating the right-hand side of each equation gives:

$$\left(\frac{1}{f}\right)\bar{A} - \left(\frac{1-c}{f}\right)Y = \left(\frac{k}{h}\right)Y - \left(\frac{1}{h}\right)\bar{M}$$

Collecting the terms in Y gives:

$$\left[\frac{k}{h} + \frac{1-c}{f}\right]Y = \left(\frac{1}{f}\right)\bar{A} + \left(\frac{1}{h}\right)\bar{M}$$

or:

$$\left[\frac{fk + h(1-c)}{hf}\right]Y = \left(\frac{1}{f}\right)\bar{A} + \left(\frac{1}{h}\right)\bar{M}$$

Hence equilibrium Y is given by:

$$\begin{aligned} Y &= \frac{hf}{fk + h(1-c)} \left[ \left(\frac{1}{f}\right)\bar{A} + \left(\frac{1}{h}\right)\bar{M} \right] \\ &= \frac{hf}{fk + h(1-c)} \left[ \frac{1}{hf} (h\bar{A} + f\bar{M}) \right] \\ &= \frac{1}{fk + h(1-c)} [h\bar{A} + f\bar{M}] \end{aligned} \quad (3)$$

and given the value for  $Y$  from Equation (3) the equilibrium value for  $i$  can be determined from the LM Equation (2).

**Example** Equilibrium in the IS-LM model

Suppose that, in a given economy,  $A = 1,010$ ,  $M = 910$ ,  $c = 0.8$ ,  $f = 1,000$ ,  $h = 1,000$  and  $k = 0.2$ . Use the IS-LM model to find the equilibrium values for  $Y$  and  $i$ .

Using Equation (3) in Box 23.3 we get:

$$Y = \frac{1}{400} \left[ (1,000) 1,010 + (1,000) 910 \right] = 4,800$$

Substituting the equilibrium value for  $Y$  into the LM equation gives the equilibrium rate of interest:

$$i = \frac{1}{1,000} \left[ 0.2 (4,800) - 910 \right] = 0.05$$

Hence in equilibrium  $i = 0.05$  and  $Y = 4,800$ . For example, in Figure 23.5, point  $E$  corresponds to an  $(i, Y)$  combination  $(0.05, 4,800)$ .

